

SPECTRA OF THE ALKALI METAL ATOMS

doublets, were obtained in absorption as in the following table and in fig. 1. Several forbidden lines were observed. The greatest n measured and the temperature depended strongly upon the temperature.

	K, $4s-np$	Rb, $5s-np$	Cs, $6s-np$
... ..	76	73	65
at	14	22	15

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ON THE ENERGY LEVELS OF A MODEL
OF THE COMPRESSED HYDROGEN ATOM

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Summary

In the problem of the "compressed hydrogen atom" the boundary condition that the wave function φ must be zero for infinite r , is replaced by the condition that φ must have a zero point at a finite $r = r_0$. This leads to an investigation of properties of the zeros of the confluent hypergeometric function. The shifts of the $1s$, $2s$ and $2p$ levels by compression are calculated and tables and graphs are given for corresponding values of the energy and of r_0 .

§ 1. *Introduction.* In the usual treatment of the Schrödinger equation for the hydrogen atom the boundary conditions imposed on the wave function φ are: regular behaviour in the origin and a node at infinity. It will however be supposed here that the hydrogen atom is enclosed in a sphere of radius r_0 ^{1) 2)}. At the position r_0 is an infinitely high and steep potential wall. So the wave function must now have a zero point at $r = r_0$ instead of at $r = \infty$. The new boundary condition influences only the radial part $R(r)$ of the wave function. The equation for $R(r)$ can be written in atomic units ^{*)}:

$$\frac{d^2 R}{dr^2} + \frac{2}{r} \frac{dR}{dr} + \left\{ 2E + \frac{2}{r} - \frac{l(l+1)}{r^2} \right\} R = 0, \quad (1)$$

with E the energy and l zero or a positive integer.

With the relations

$$\rho = 2r/n \text{ and } E = -1/2n^2, \quad (2)$$

^{*)} Fundamental units e , m , and $\hbar = h/2\pi$. The unit of length is then $a_0 \equiv \hbar^2/me^2$ and the unit of energy is e^2/a_0 (Michels, De Boer and Bijl¹⁾ take $e^2/2a_0$ as unit of energy).

REFERENCES

- Mac k, Rev. Mod. Physics, **14**, 104, 1942.
Mac k, Journ. Opt. Soc. Am. **32**, 457, 1942.